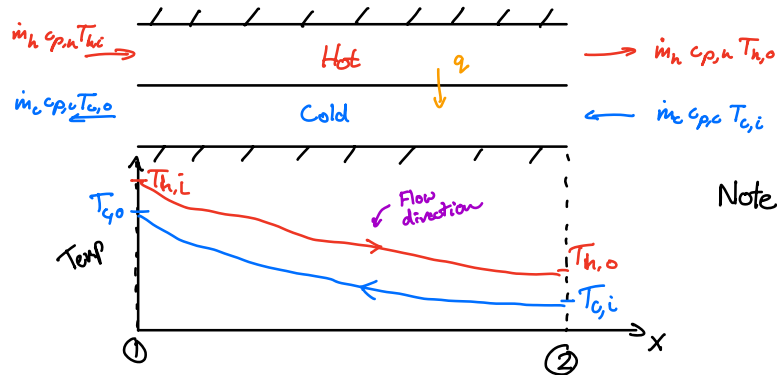


13A - 2ND CLASS

Counterflow HX



Note: $T_{c,o}$ can be greater than $T_{h,o}$

Analysis:

$$q = \dot{m}_h c_{p,h} (T_{h,i} - T_{h,o})$$

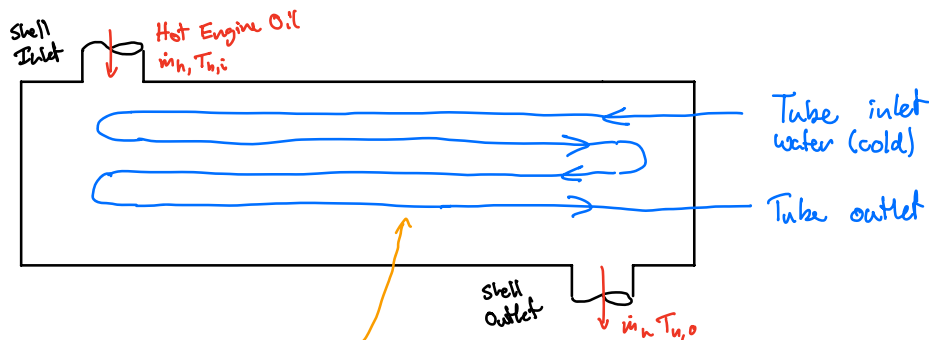
$$q = \dot{m}_c c_{p,c} (T_{c,o} - T_{c,i})$$

$$q = U A \Delta T_{lm} \quad \Delta T_{lm} = \frac{\Delta T_2 - \Delta T_1}{\ln(\Delta T_2 / \Delta T_1)}$$

$$\Delta T_2 = T_{h,o} - T_{c,i}$$

$$\Delta T_1 = T_{h,i} - T_{c,o}$$

see Table 11.3 for $\epsilon = f(NTU, Cr)$



$N = \text{number of brass tubes} = 11$ there are 11 tubes along this path

1 shell pass
4 tube pass

Engine Oil

$$T_{h,i} = 160^\circ\text{C}$$

$$T_{h,o} = 94^\circ\text{C}$$

Water

$$\dot{m}_c = 10,000 \text{ kg/hr}$$

$$T_{c,i} = 16^\circ\text{C}$$

$$T_{c,o} = 84^\circ\text{C}$$

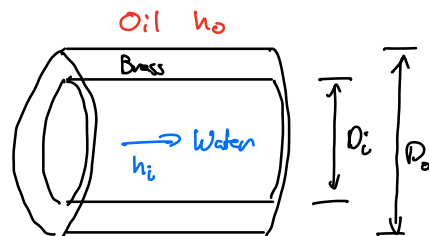
$$N = 11 \leftarrow \text{Number of brass tubes}$$

$$D_i = 22.9 \text{ mm}$$

$$D_o = 25.4 \text{ mm}$$

} Dimensions of brass tubes

$$h_o = 400 \frac{\text{W}}{\text{m}^2\text{K}}$$



1. Number of mass transfer unit (NTU)?

$$NTU = ?$$

$$NTU = \frac{UA}{C_{min}} \rightarrow \text{Table 11.4} \rightarrow NTU = -(1 + Cr^2)^{-1/2} \ln \left(\frac{E-1}{E+1} \right)$$

for 1 shell pass
(2, 4, ..., tube passes)

$$E = \frac{\frac{2}{E} - (1 + Cr)}{(1 + Cr^2)^{1/2}}$$

$$Cr = \frac{C_{min}}{C_{max}} \quad E = \frac{2}{2_{conv}}$$

heat capacity rate
 $C \equiv \dot{m} c_p$

$$C_c = \dot{m}_c c_{p,c}$$

$\rightarrow$

Evaluate water at

$$\overline{T}_c = \frac{T_{c,i} + T_{c,o}}{2} = 50^\circ\text{C}$$

$\Rightarrow$ Table A-6 @ 323 K, Interpolate:

specific volume $\rightarrow \overline{V}_f = 1.0122 \times 10^{-3} \text{ m}^3/\text{kg} \quad \rightarrow \beta_f = \frac{1}{\overline{V}_f}$

$$k_w = 0.643 \frac{\text{W}}{\text{m}\cdot\text{K}}$$

$$c_p = 4181.2 \frac{\text{J}}{\text{kg}\cdot\text{K}}$$

$$\mu = 5.476 \times 10^{-4} \text{ kg/m}\cdot\text{s}$$

$$Pr = 3.56$$

$$So, C_c = 11,614.4 \text{ W/K}$$

Recall,

$$q = C_c (T_{c,o} - T_{c,i}) = 7.898 \times 10^5 \text{ W}$$

$$q = C_h (T_{h,i} - T_{h,o})$$

$$C_h = \frac{q}{T_{h,i} - T_{h,o}} = 11,966.4 \text{ W/K}$$

$$C_{min} = C_c$$

$$C_r = \frac{C_{min}}{C_{max}} = 0.971$$

$$\epsilon = \frac{q}{q_{max}} = \frac{q}{C_{min}(T_{h,i} - T_{c,i})}$$

$$\epsilon = 0.472$$

$$E = \dots = 1.625$$

$$NTU = \dots = 1.03$$

2. Find the U based on area A_o